### Amended Section of Page 2 Corresponding to the Last Paragraph

The procedure of the Fiat-Shamir scheme can be expounded as follows. A reliable system administrator selects a sufficiently large number n. Then, A prover selects his own private key a that is relatively prime with n, and calculates  $b = a^2 \mod n$ . The prover discloses b. Then, the following protocol is repeated for a number of times:

- (a) The prover selects a random integer  $r Z_n^*$   $r \in Z_n^*$ , where  $Z_n^*$  is a multiplicative group of order n, calculates  $x = r^2$ , and sends x to the verifier;
- (b) The verifier selects a random number  $\Box \Box \{0,1\}$   $\underline{\varepsilon} \subseteq \{0,1\}$ , and sends  $\Box \subseteq$  to the prover;
- (c) On receiving  $\oplus \underline{\varepsilon}$ , the prover calculates  $y = r \oplus a^{\oplus} \underline{y} = r \cdot \underline{a}^{\varepsilon} \mod n$  and sends y to the verifier; and
- (d) The verifier examines whether  $y^2 = x \Box b^{\Box} \underline{y^2 = x \cdot b^{\varepsilon}} \mod n$  is established. If true, then the verifier accepts the prover as a legitimate user and, otherwise, stops the protocol.

### Amended Section of Page 3 Corresponding to the First Two Paragraphs

Various schemes have been developed based on the original Fiat-Schamir scheme, and follows the above-mentioned protocol.

On the other hand, the procedure of the Schnorr scheme is as follows. First, two primes numbers p and q are chosen, wherein q is a prime factor of p-1. Then, choose a not equal to 1, such that  $a^q \oplus 1 \pmod{p}$   $a^q \oplus 1 \pmod{p}$ . Then, a random number s, i.e., the private key, less than q is chosen. The public key  $v = a^{-s} \mod p$  is then calculated. Thereafter, the following protocol is executed:

- (a) The prover selects a random number r less than q, and computes  $x = a^r$  mod p, then sends x to the verifier;
- (b) The verifier sends the prover a random number  $\Box \Box Z_q^* \underline{\varepsilon} \subseteq Z_q^*$ , where  $Z_q^*$  is a multiplicative group of order q;
- (c) The prover computes  $y = r + s \square \mod q$   $y = r + s \varepsilon \mod q$  and sends y to the verifier; and
- (d) The verifier verifies whether  $x = a^y \Box v^{\Box} x = a^y \cdot v^c \mod p$  is established. If true, then the verifier accepts the prover as a legitimate user and, otherwise, stops the protocol.

# Amended Section of Page 5 Corresponding to Line 2 and Line 18

 $\Box Z_m^* \subseteq Z_m^*$  to obtain a query R, storing the evidence (x, Q) and the randomly selected number

selected number  $\omega \oplus Z_m^*$   $\underline{\omega} \in Z_m^*$  to obtain a query R, storing the evidence (x,Q) and the

# Amended Section of Page 9 Corresponding to Line 10

Subsequently, the prover selects random numbers  $r_1, r_2, r_3 \Box Z_m^* r_1, r_2$ ,

 $\underline{r_3} \subseteq \underline{Z_m}^{\underline{\bullet}}$  and generates

## Amended Section of Page 10 Corresponding to Line 1

The verifier receives the evidence (x, Q), selects a randomly selected number

 $\omega \oplus \underline{\omega} \in$